

$$\begin{aligned} \log p(x) &\geq \log p(x) - D(q(y)||p(y|x)) \\ &= \int dq(y) [\log p(x) + \log p(y|x) - q(y)] \\ &= \int dq(y) \log p(x, y) + H[q] \end{aligned}$$